

# Status of the Unitarity Triangle in the Standard Model

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on behalf of the

*UTfit Collaboration*

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<http://www.utfit.org>



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# The Method and the Inputs:

The experimental inputs, function of  $\bar{\rho}$  and  $\bar{\eta}$ , are related to the  $\bar{\rho}$  and  $\bar{\eta}$  through the Bayes Theorem

$$f(\bar{\rho}, \bar{\eta}, X | c_1, \dots, c_m) \sim \prod_{j=1,m} f_j(\mathcal{C} | \bar{\rho}, \bar{\eta}, X) * \prod_{i=1,N} f_i(x_i) f_0(\bar{\rho}, \bar{\eta})$$

$$X \equiv x_1, \dots, x_n = m_t, B_K, F_B, \dots$$

$$\mathcal{C} \equiv c_1, \dots, c_m = \epsilon, \Delta m_d / \Delta m_s, A_{CP}(J/\psi K_S), \dots$$

$(b \rightarrow u)/(b \rightarrow c)$	$\bar{\rho}^2 + \bar{\eta}^2$	$\bar{\Lambda}, \lambda_1, F(1), \dots$
$\epsilon_K$	$\bar{\eta}[(1 - \bar{\rho}) + P]$	$B_K$
$\Delta m_d$	$(1 - \bar{\rho})^2 + \bar{\eta}^2$	$f_B^2 B_B$
$\Delta m_d / \Delta m_s$	$(1 - \bar{\rho})^2 + \bar{\eta}^2$	$\xi$
$A_{CP}(J/\psi K_S)$	$\sin 2\beta$	—

Standard Model +  
OPE/HQET/  
Lattice QCD  
*to go from  
quarks  
to hadrons*

$m_t$

see also: M.B., UTfit talk  
at the *Physics beyond the SM* session

M. Bona *et al.* (UTfit Collaboration)  
JHEP07(2005) 028 hep-ph/0501199

# Inputs used

New values  
but WA not  
available yet

**new from  
HFAG**

**new from  
the Tevatron**

**new value  
from LQCD**

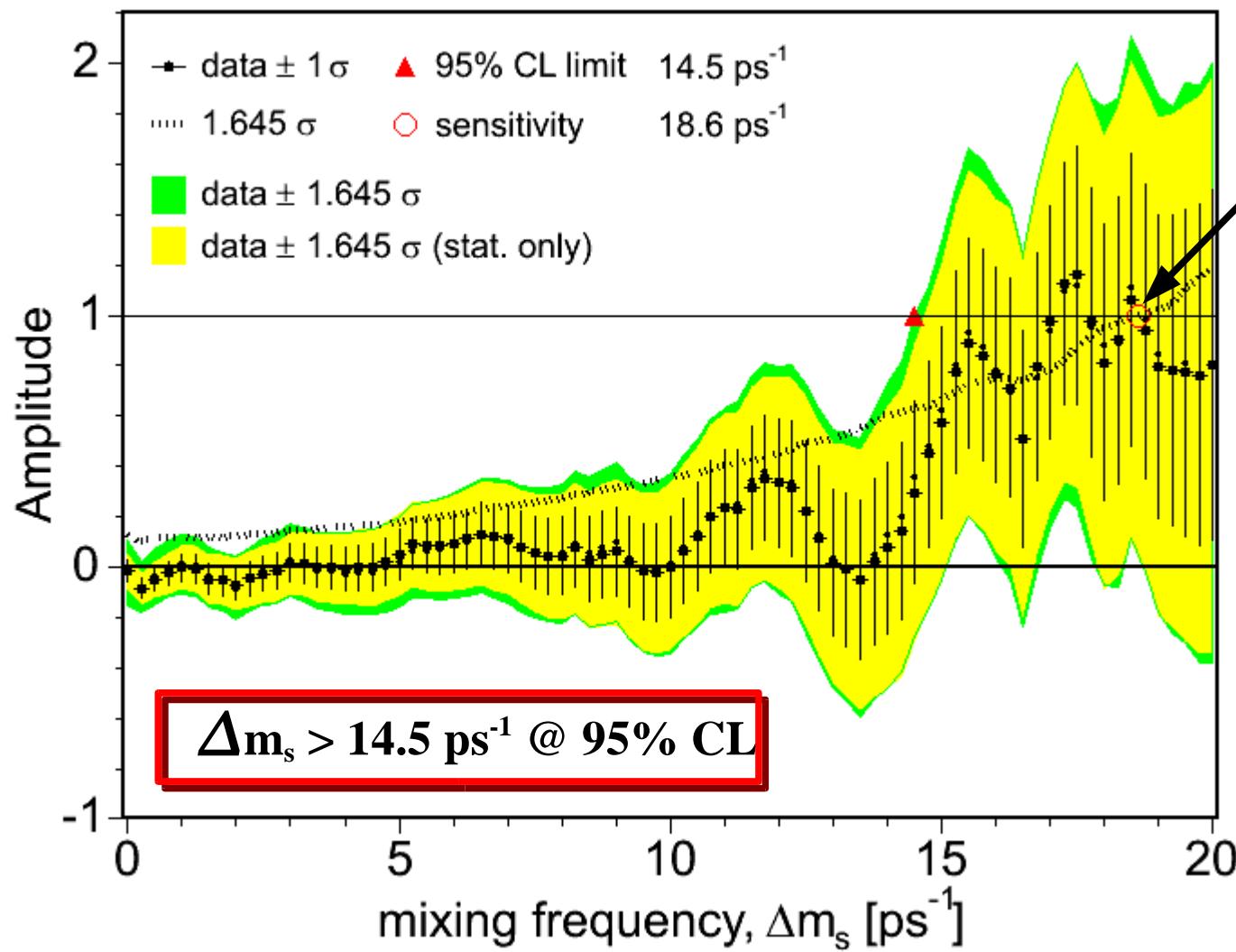
**new WA**

flat error

$\lambda$	$0.2258 \pm 0.0014$	
$V_{cb}$ inclusive	$41.6 \pm 0.7 \pm 0.6 \cdot 10^{-3}$	average from inclusive
$V_{cb}$ exclusive	$41.4 \pm 2.1 \cdot 10^{-3}$	average from exclusive
$V_{ub}$ inclusive LEP	$4.09 \pm 0.62 \pm 0.47 \cdot 10^{-3}$	LEP average
$V_{ub}$ inclusive HFAG	$4.38 \pm 0.19 \pm 0.27 \cdot 10^{-3}$	LP05
$V_{ub}$ exclusive	$3.80 \pm 0.27 \pm 0.47 \cdot 10^{-3}$	BR from HFAG + LQCD
$\Delta m_d$	$0.502 \pm 0.007 \text{ ps}^{-1}$	LEP/SLD/CDF/B-Factories
$\Delta m_s$	$> 14.5 \text{ ps}^{-1}$	LEP/SLD/CDF-1
$m_t$	$165.0 \pm 3.9 \text{ GeV}$	CDF/D0 (LP05)
$m_c$	$1.3 \pm 0.1 \text{ GeV}$	
$f_{B_s} \sqrt{\hat{B}_{B_s}}$	$276 \pm 38 \text{ MeV}$	Lattice QCD
$\xi$	$1.24 \pm 0.04 \pm 0.06$	Lattice QCD
$B_K$	$0.79 \pm 0.04 \pm 0.09$	Lattice QCD
$\sin 2\beta$	$0.687 \pm 0.032$	B-Factories

# New Likelihood for $\Delta m_s$

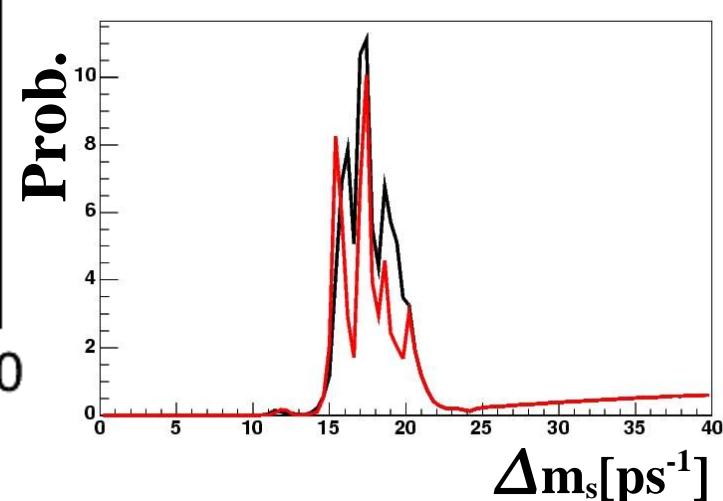
World Average and CDF II



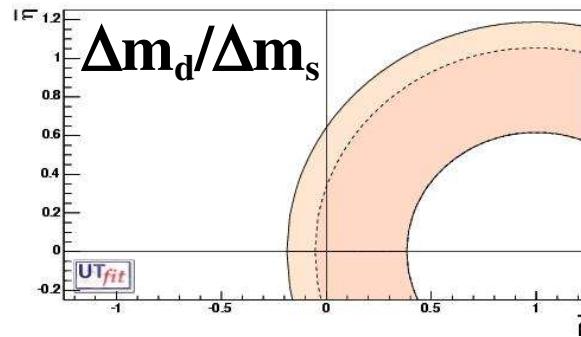
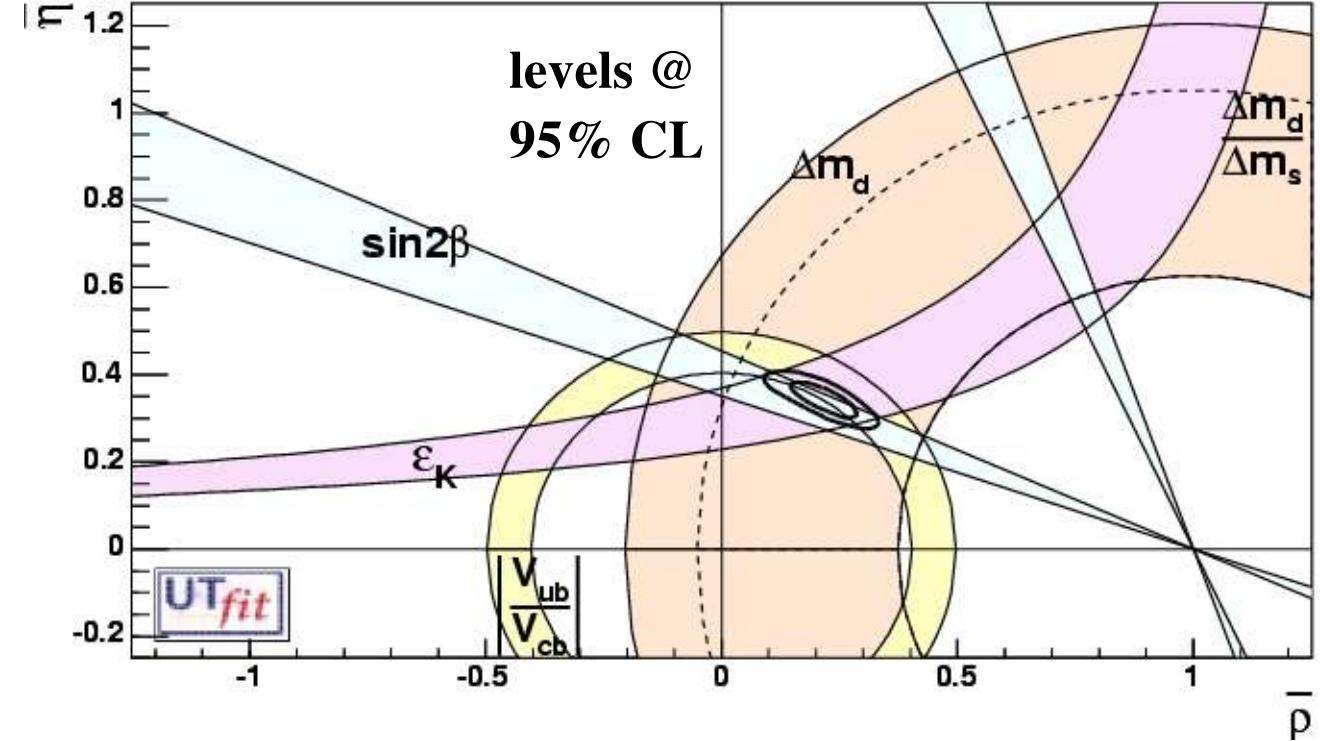
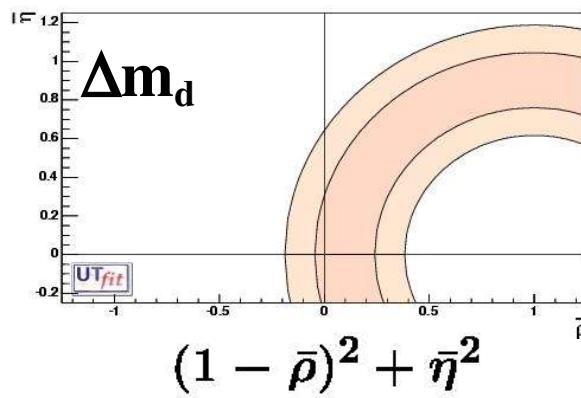
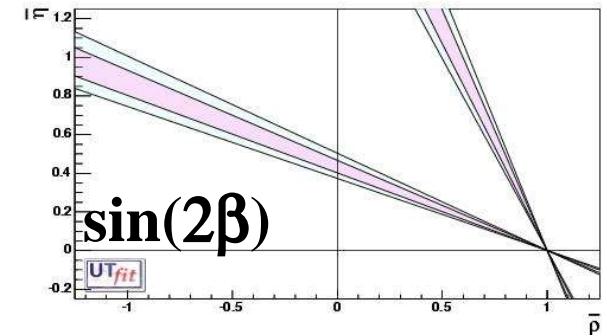
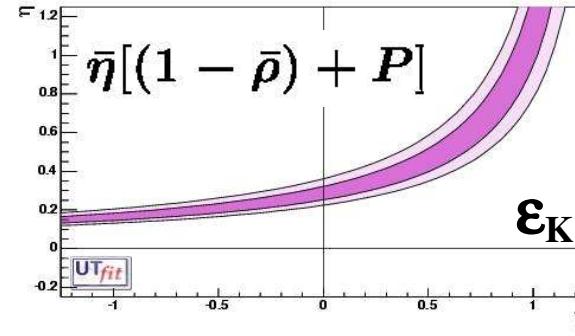
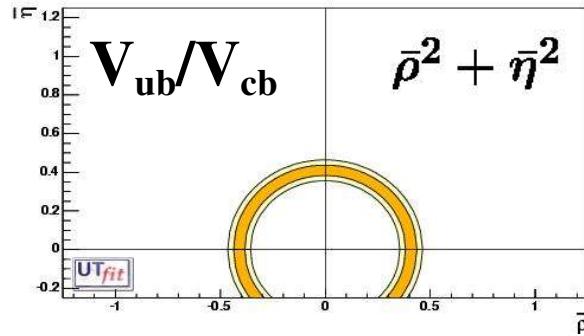
$$P_{B_q^0 \rightarrow B_q^0(\bar{B}_q^0)} = \frac{1}{2} e^{-t/\tau_q} (1 \pm A \cos \Delta m_q t)$$

signal *hint* @  
 $\Delta m_s \sim 18.6 \text{ ps}^{-1}$  with  
~ $2\sigma$  stat. significance

black: before CKM2005  
red: after CKM2005



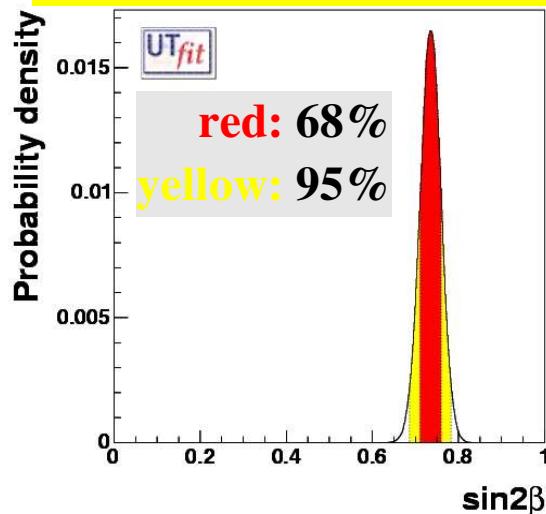
# Standard constraints in the $\bar{\rho}$ - $\bar{\eta}$ plane:



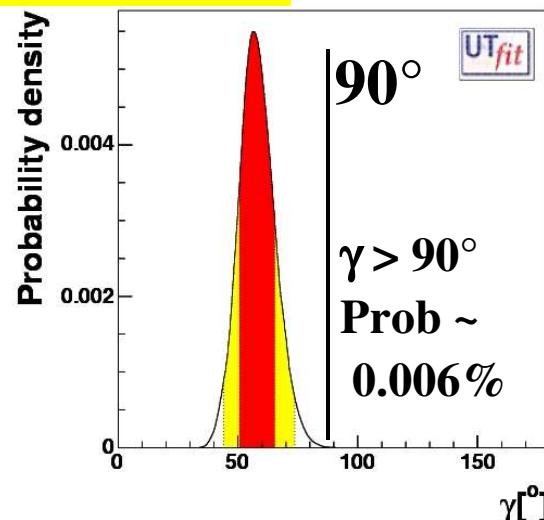
$\bar{\rho} = 0.214 \pm 0.047$   
 $[0.112, 0.307] @ 95\% \text{ Prob.}$

$\bar{\eta} = 0.343 \pm 0.028$   
 $[0.289, 0.396] @ 95\% \text{ Prob.}$

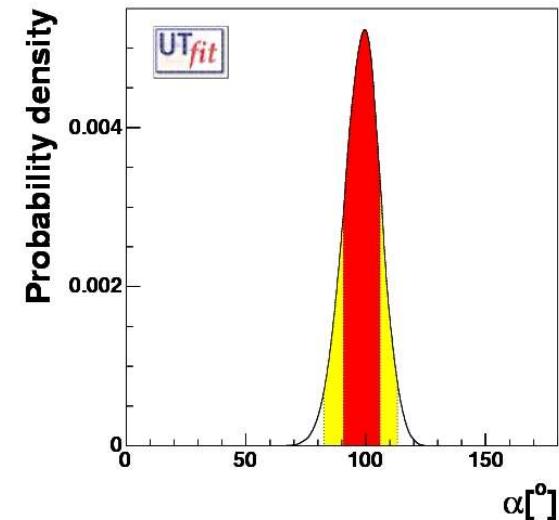
# Indirect determinations:



$\sin 2\beta = 0.734 \pm 0.024$   
 $[0.685, 0.781] @ 95\% \text{ Prob.}$



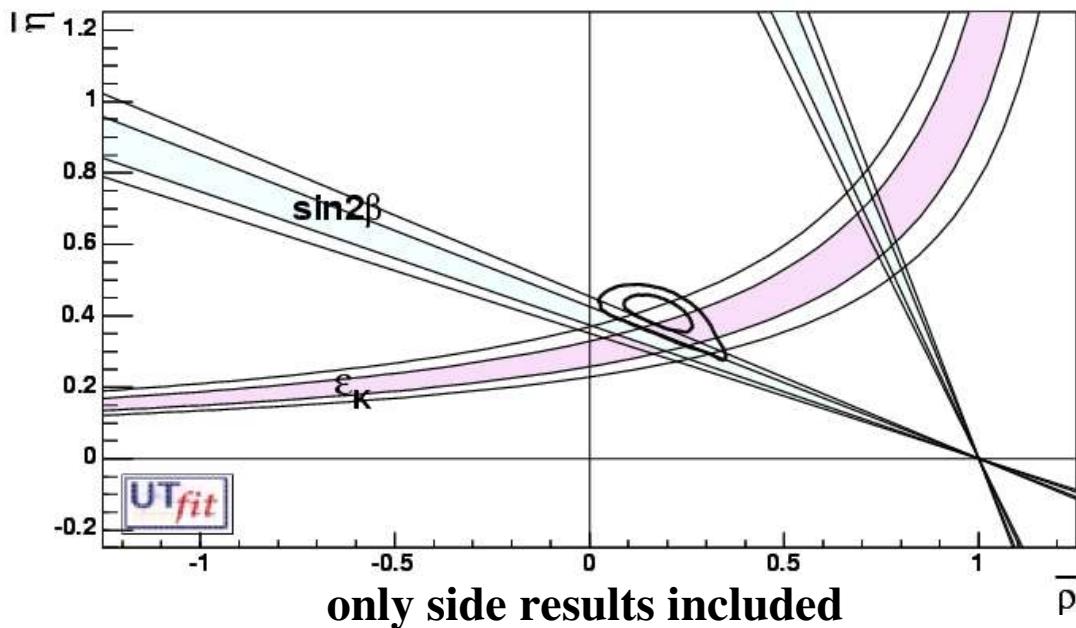
$\gamma = 57.9^\circ \pm 7.4^\circ$   
 $[43.8, 73.5]^\circ @ 95\% \text{ Prob.}$



$\alpha = 98.2^\circ \pm 7.7^\circ$   
 $[82.4, 113.0]^\circ @ 95\% \text{ Prob.}$

*from experiment*  
 $\sin 2\beta = 0.687 \pm 0.032$

*from the only-side fit*  
 $\sin 2\beta = 0.793 \pm 0.033$



**$V_{ub}$** **exclusive value:**

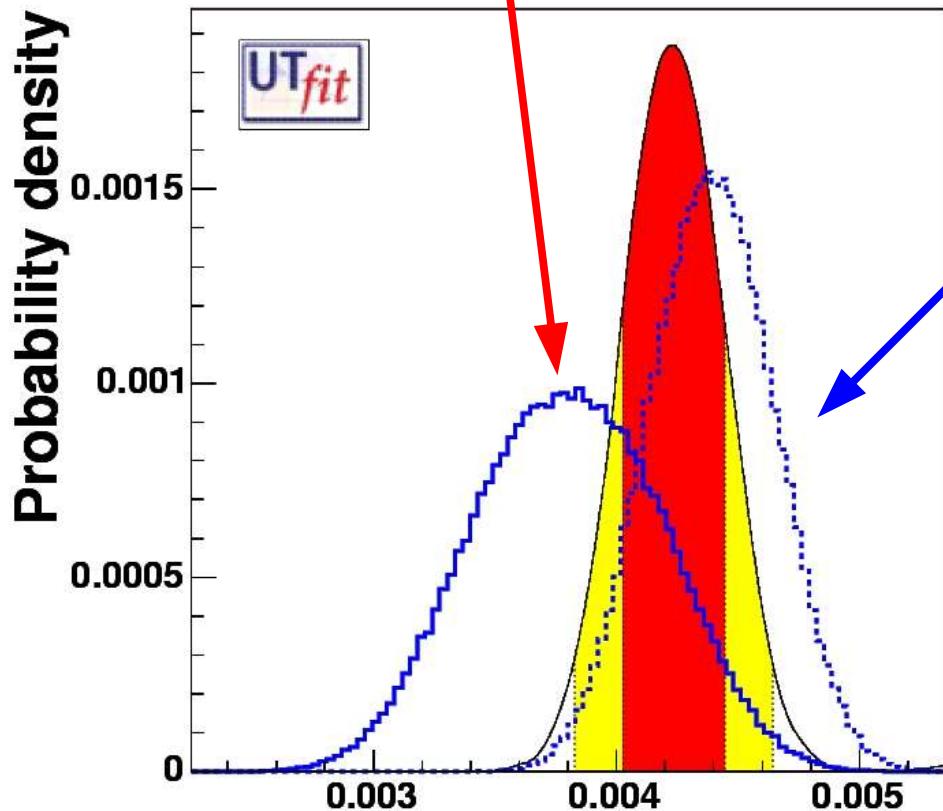
semileptonic BRs from HFAG

form factor (courtesy of V. Lubicz)

$$V_{ub} = (3.80 \pm 0.27 \pm 0.47) 10^{-3}$$

**inclusive value: from HFAG**

$$V_{ub} = (4.38 \pm 0.19 \pm 0.27) 10^{-3}$$

**mediating:**

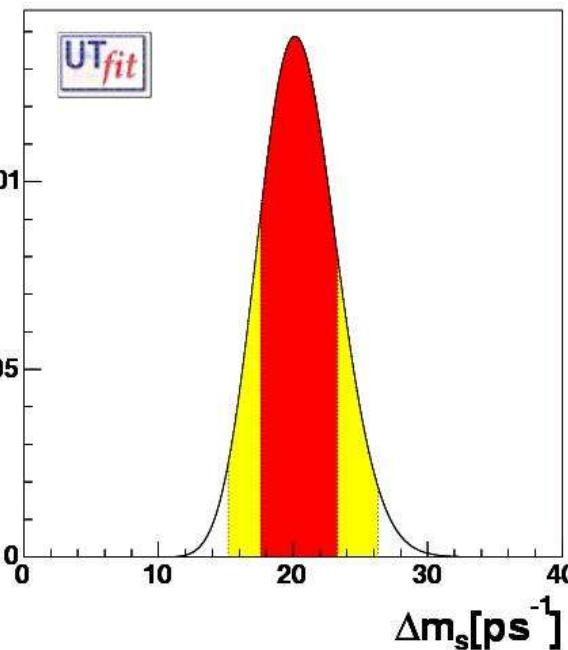
$$V_{ub} = (4.22 \pm 0.20) 10^{-3}$$

 **$V_{ub}$** **from all the other inputs:**

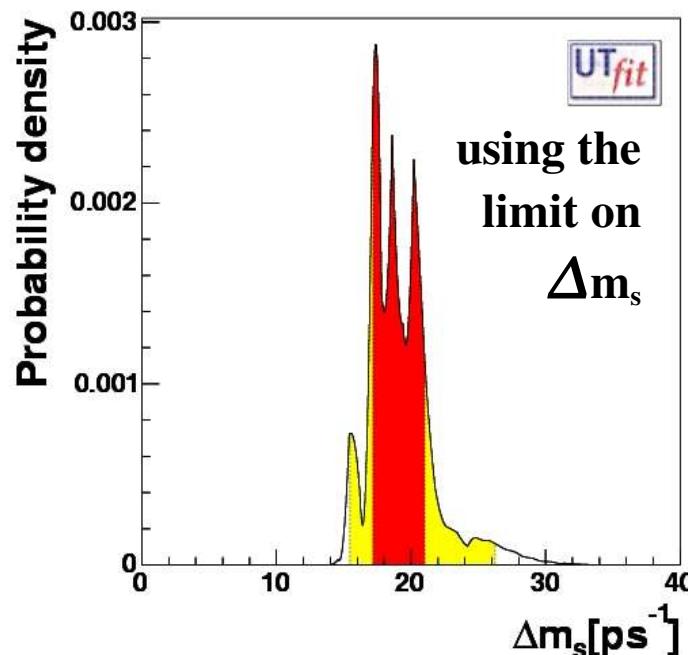
$$V_{ub} = (3.48 \pm 0.20) 10^{-3}$$

 **$V_{ub}$**

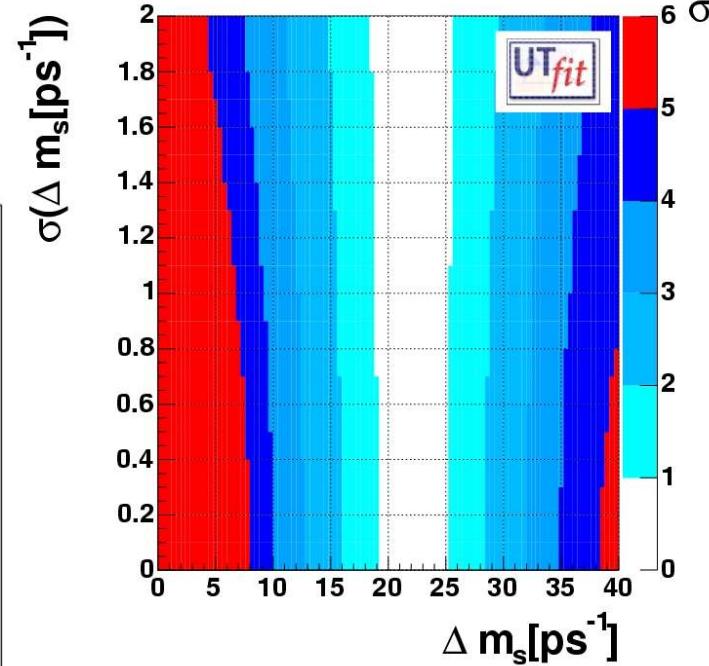
# Prediction on $\Delta m_s$ and test on the SM



$\Delta m_s = 22.2 \pm 3.1 \text{ ps}^{-1}$   
without the  
experimental bound



$\Delta m_s = 19.1 \pm 2.0 \text{ ps}^{-1}$   
with the  
experimental bound



$\Delta m_s > 31 \text{ ps}^{-1}$   
New Physics @  $3\sigma$   
[for  $\sigma(\Delta m_s) \sim 1 \text{ ps}^{-1}$ ]



# and LQCD predictions

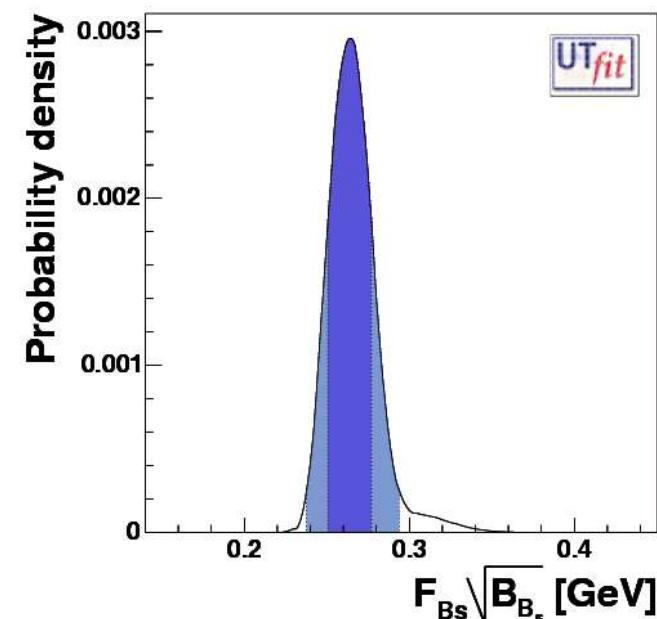
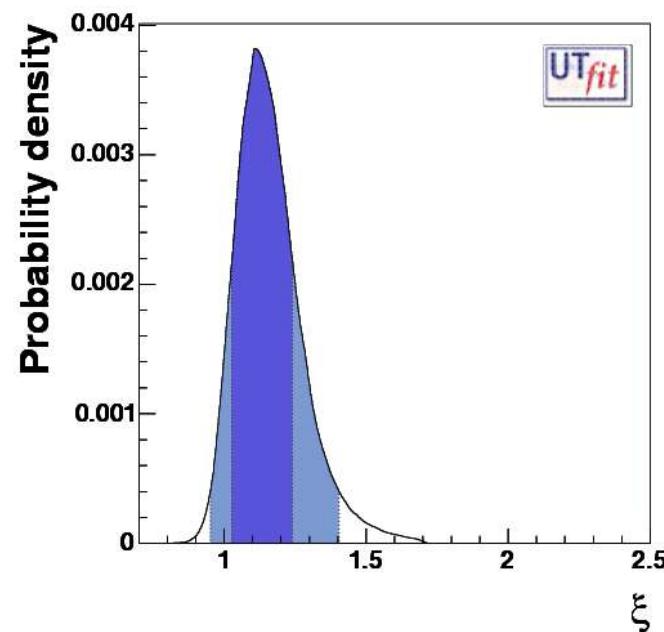
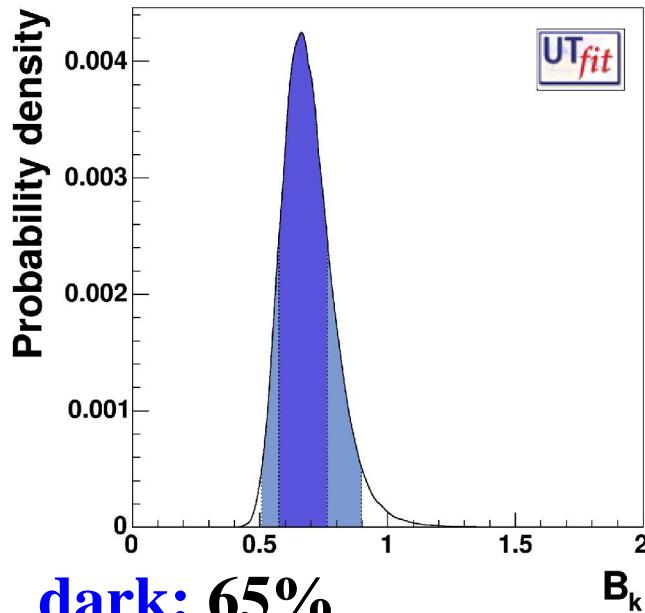
It is possible to obtain predictions on lattice QCD parameters employing all the other inputs

$$B_K = 0.69 \pm 0.10$$



$$B_K = 0.79 \pm 0.04 \pm 0.09$$

LQCD



$$f_{B_s} \sqrt{B_{B_s}} = 265 \pm 13$$

$$f_{B_s} \sqrt{B_{B_s}} = 276 \pm 38$$



light: 95%

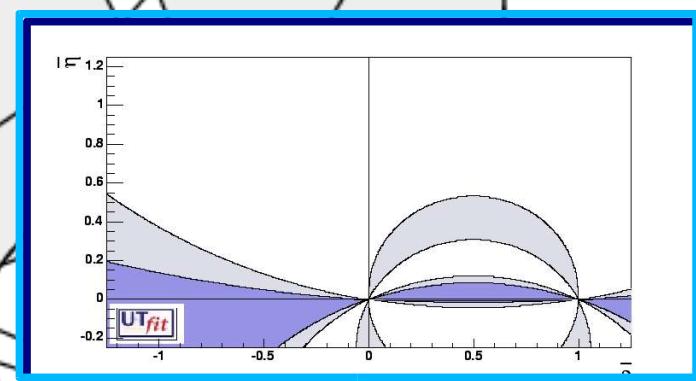
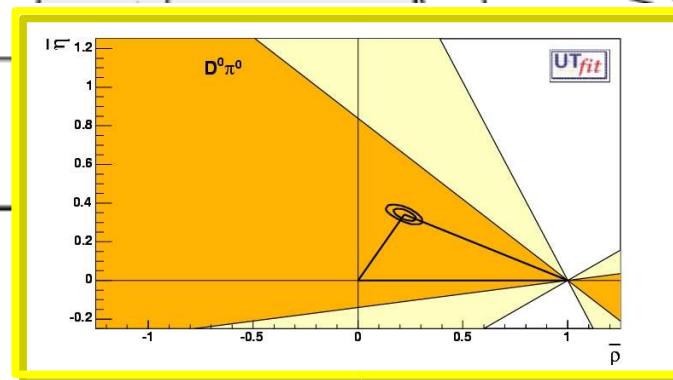
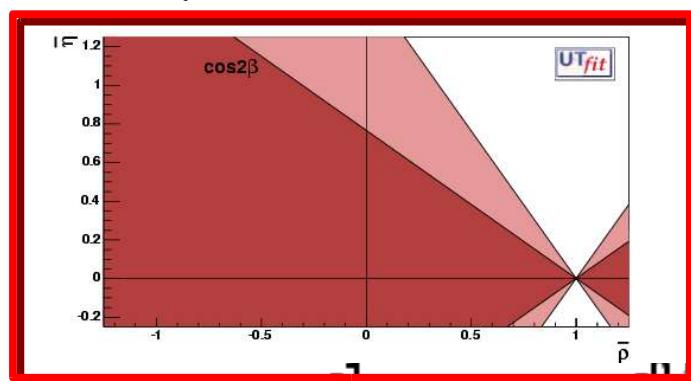
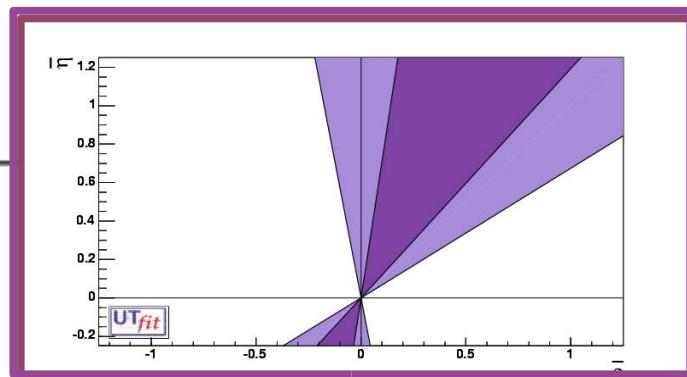
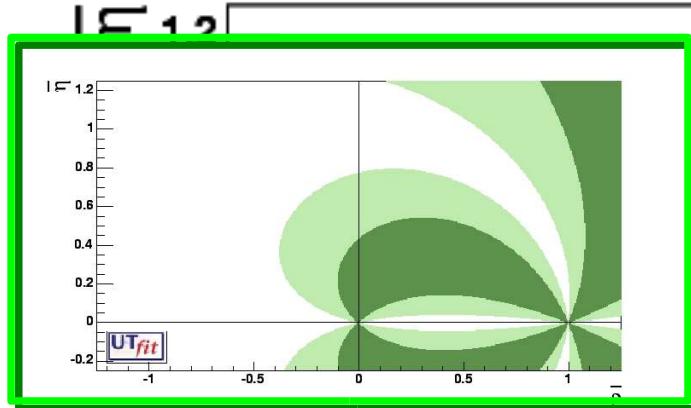
$$\xi = 1.15 \pm 0.11$$



$$\xi = 1.24 \pm 0.04 \pm 0.06$$

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# New Constraints



## $\alpha$ from isospin analysis: $\pi\pi$ , $\rho\rho$ , $\rho\pi$

Starting from the SU(2) amplitudes ( $\pi\pi$ ,  $\rho\rho$ ):

$$A^{+-} = -Te^{-i\alpha} + Pe^{i\delta_P}$$

$$A^{+0} = -1/\sqrt{2} e^{-i\alpha} (T + T_C e^{i\delta_C})$$

$$A^{00} = -1/\sqrt{2} (T_C e^{i\delta_C} e^{-i\alpha} + Pe^{i\delta_P})$$

unknowns:  $T$ ,  $P$ ,  $T_C$ ,  $\delta_P$ ,  $\delta_{T_C}$ ,  $\alpha$

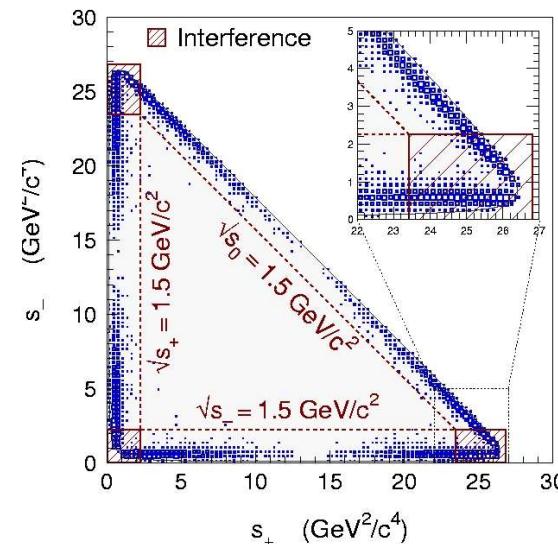
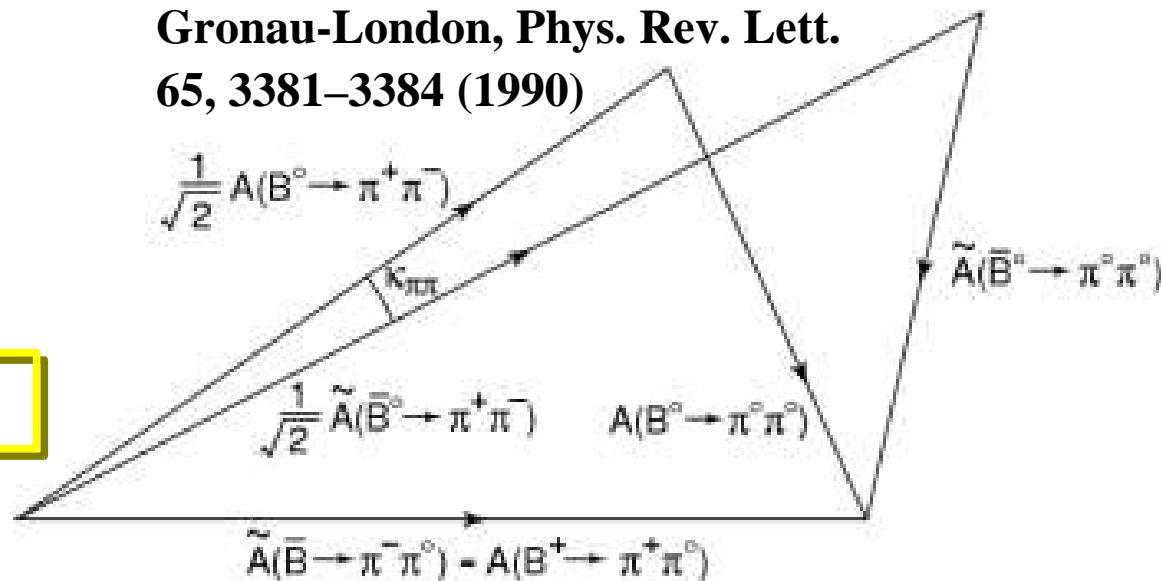
observable: 3x BR,  $C_{+-}$ ,  $S_{+-}$ ,  $C_{00}$

Similar analysis for  $(\rho\pi)^0$  on the Dalitz plane

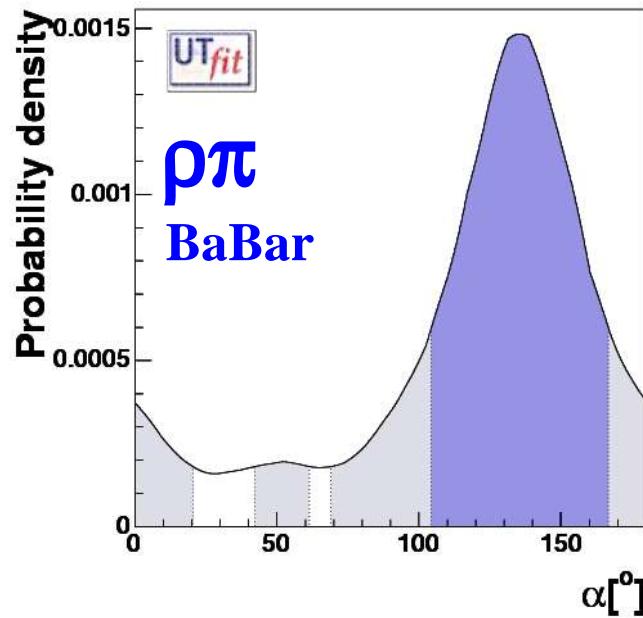
$$A^k = T^k e^{-i\alpha} + P^k$$

$$\bar{A}^k = T^k e^{i\alpha} + P^k$$

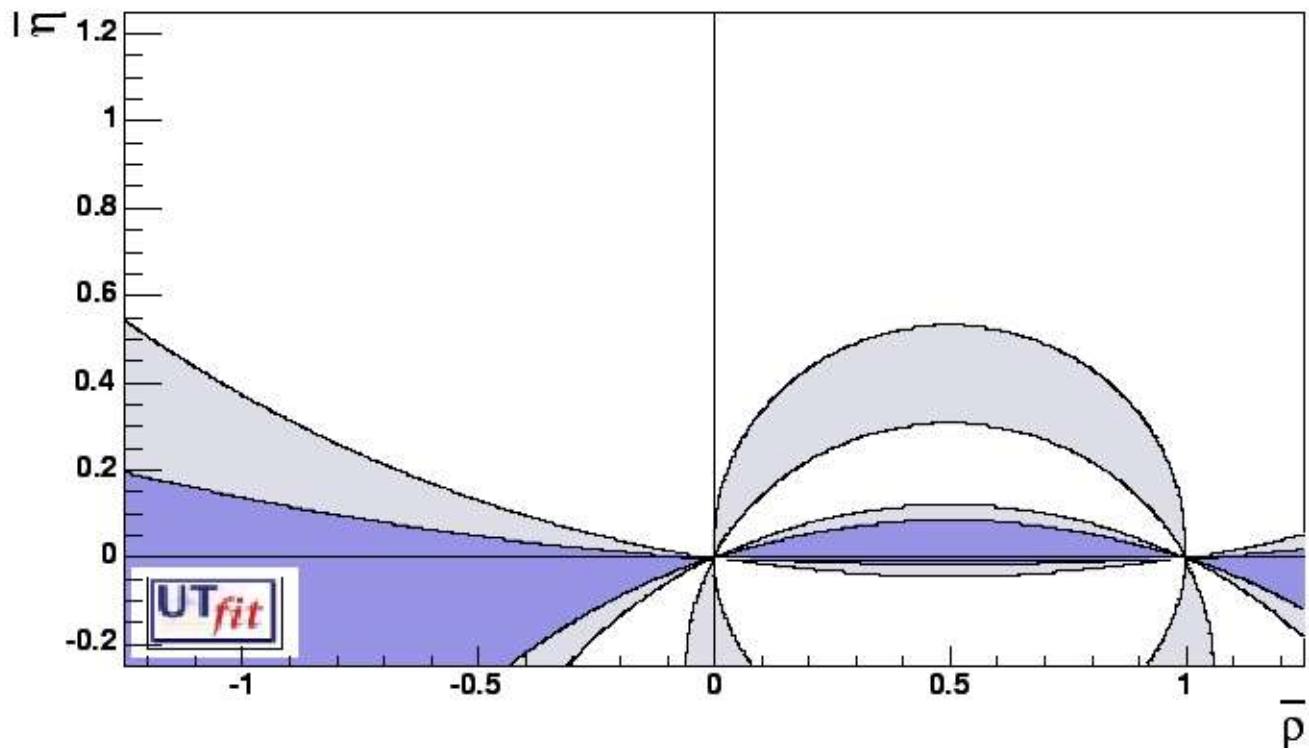
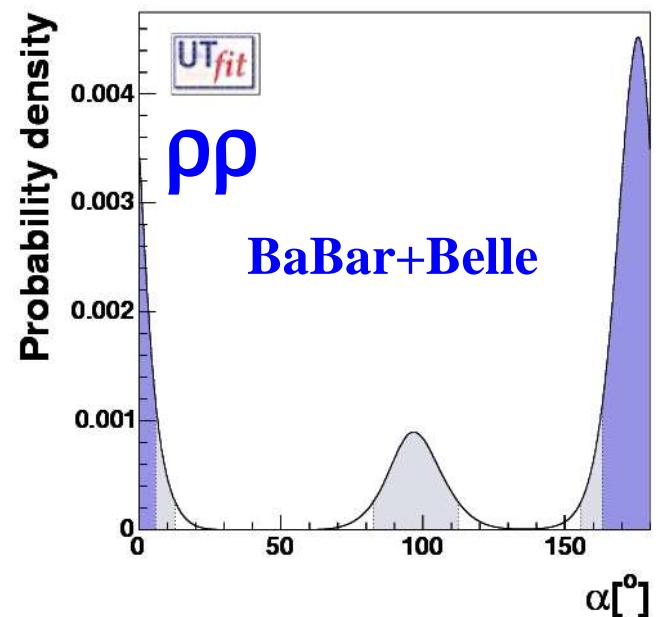
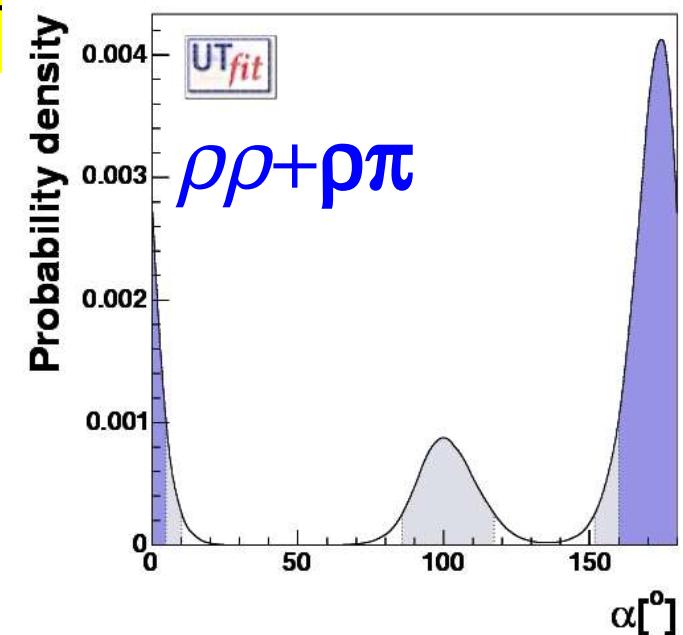
with  $k=+-$  for  $\rho^+\pi^-$ ,  $-+$  for  $\rho^-\pi^+$ ,  
 $= 00$  for  $\rho^0\pi^0$



## $\alpha$ from isospin analysis (II): $\rho\rho$ , $\rho\pi$



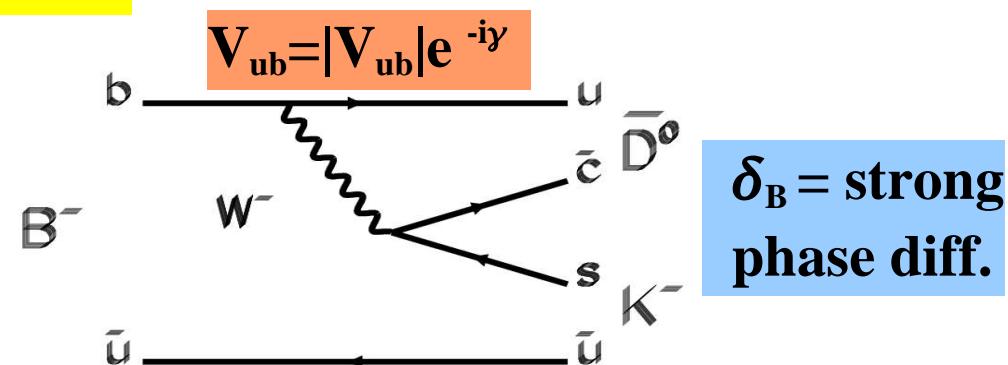
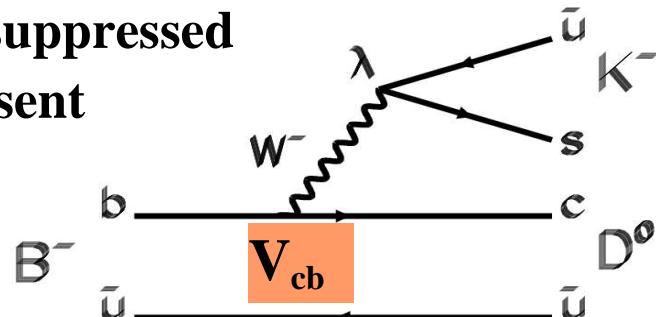
$\alpha = [86, 107]^\circ$   
 $U$   
 $[152, 90]^\circ$   
@ 95% Prob.



# $\gamma$ : from $B \rightarrow D^{(*)}K^{(*)}$ decays

also the color-suppressed diagram is present

$r_B$  = ratio of amplitudes



$$A(B^- \rightarrow D^0 K^-) = A_B \quad A(B^- \rightarrow \bar{D}^0 K^-) = A_B r_B e^{i(\delta_B - \gamma)}$$

$$A(B^+ \rightarrow \bar{D}^0 K^+) = A_B \quad A(B^+ \rightarrow D^0 K^+) = A_B r_B e^{i(\delta_B + \gamma)}$$

ADS(Atwood,Dunietz,Soni) method:  $B^0$  and  $\bar{B}^0$  into the same final state

$$R_{ADS} = r_B^2 + r_{DCS}^2 + 2r_B r_{DCS} \cos \gamma \cos(\delta_B + \delta_D)$$

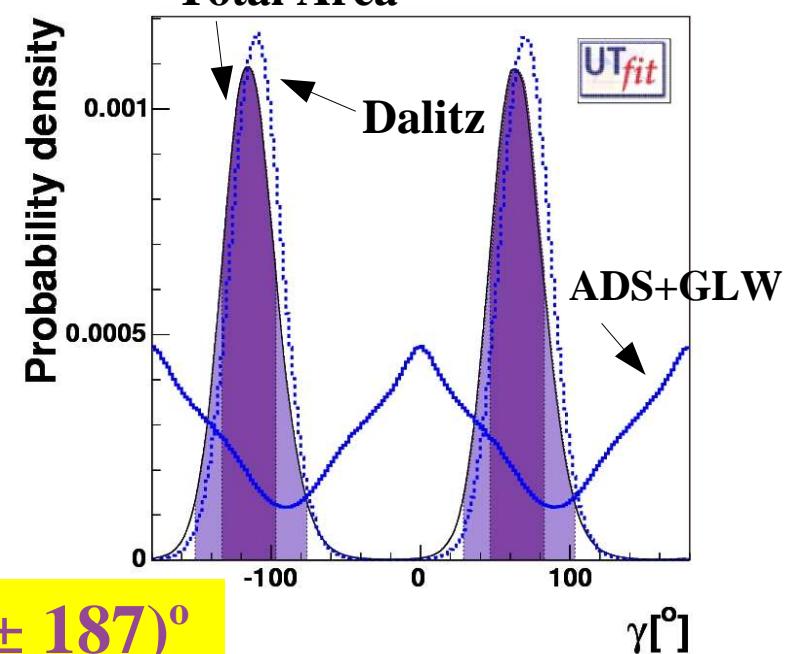
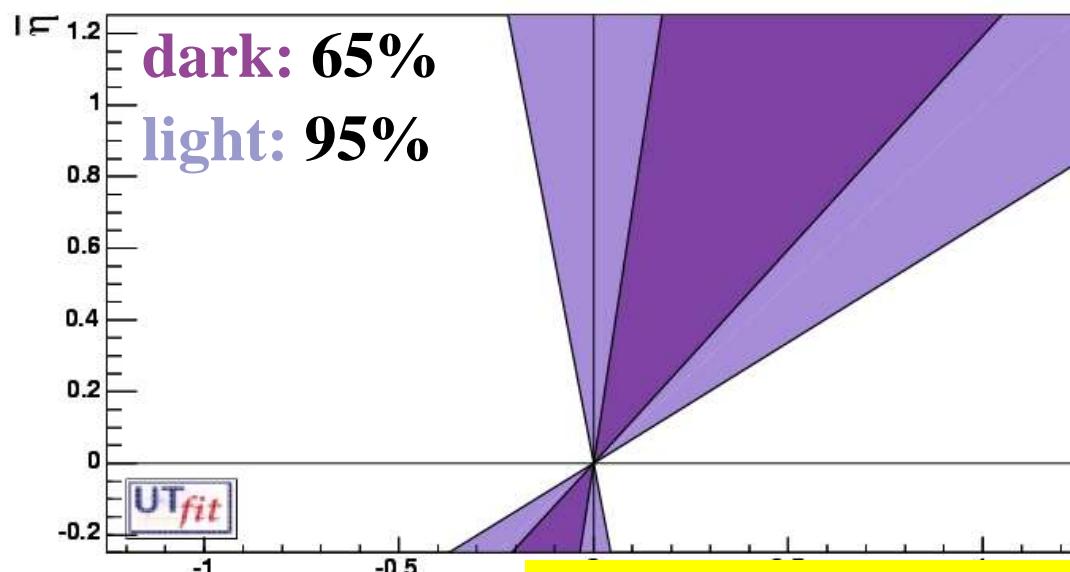
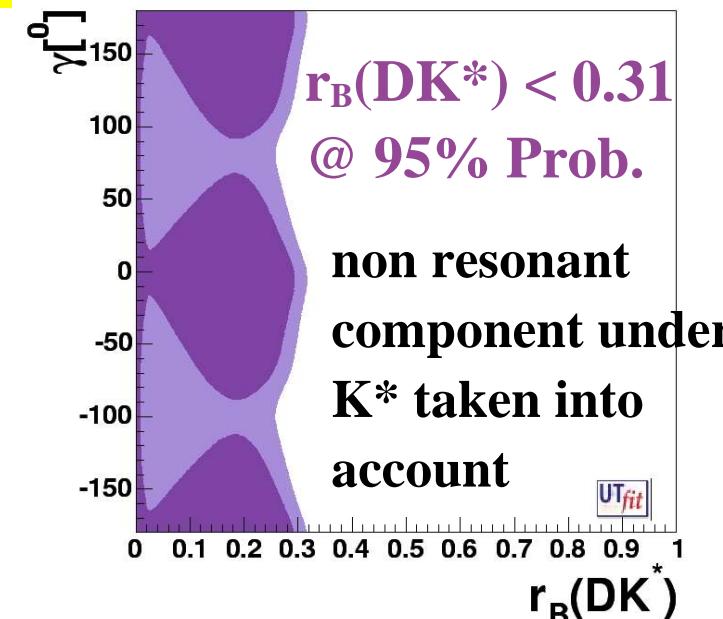
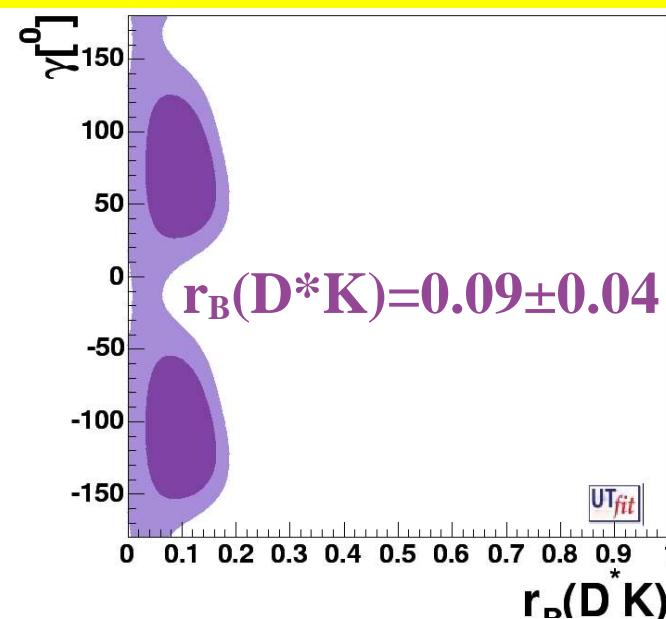
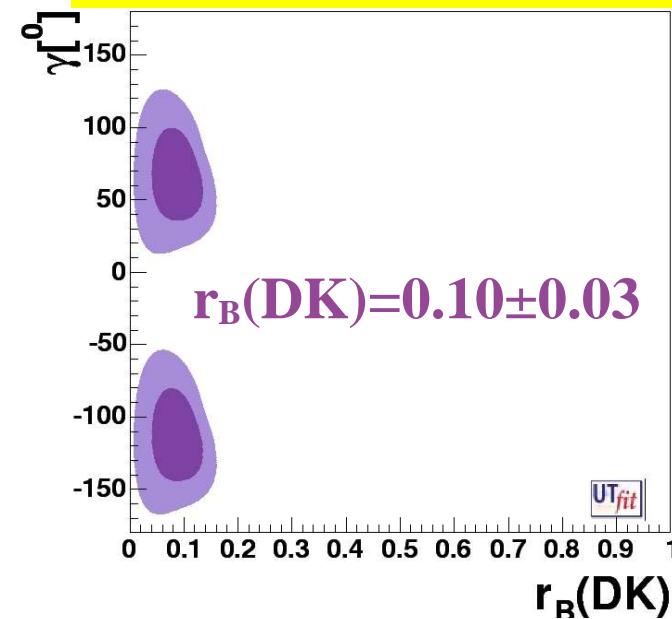
GLW(Gronau, Londow,Wyler) method: looks for the CP eigenstates of the D

$D^{(*)0}_{CP}$

$$R_{CP\pm} = 1 + r_B^2 \pm 2r_B \cos \gamma \cos \delta_B \quad A_{CP\pm} = \frac{\pm 2r_B \sin \gamma \sin \delta_B}{1 + r_B^2 \pm 2r_B \cos \gamma \cos \delta_B}$$

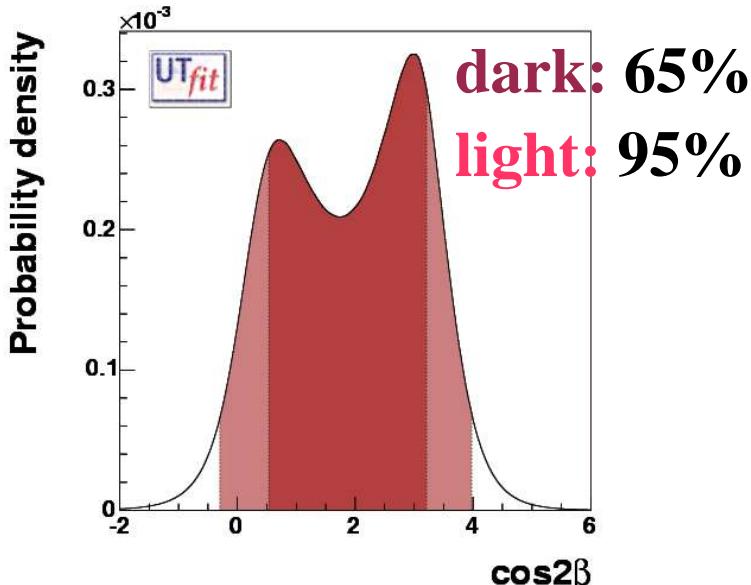
D<sup>0</sup> Dalitz plot analysis with  $B^- \rightarrow D^{(*)0}[K_S \pi^+ \pi^-] K^-$  decays

# $\gamma$ : from $B^\pm \rightarrow D(\ast)K(\ast)$ decays (II)

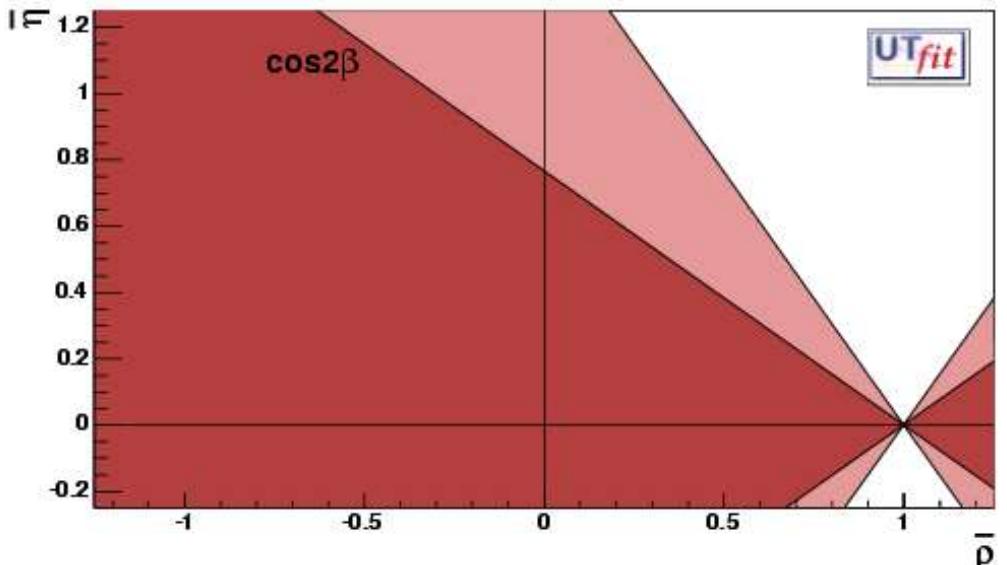


$$\gamma = (66 \pm 17)^\circ \text{ U } (-114 \pm 187)^\circ$$

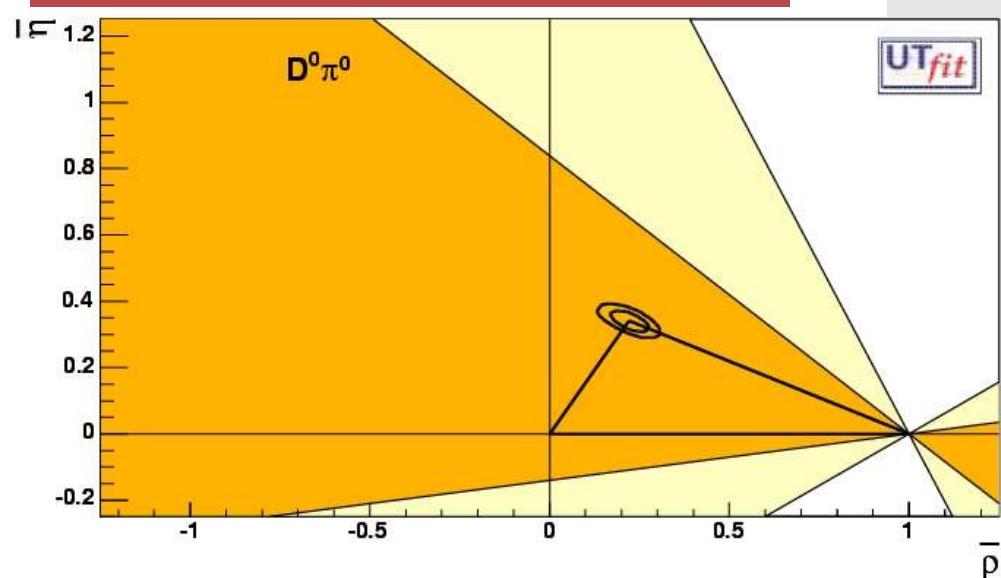
# $\cos 2\beta$ from $B \rightarrow J/\psi K^{*0}$



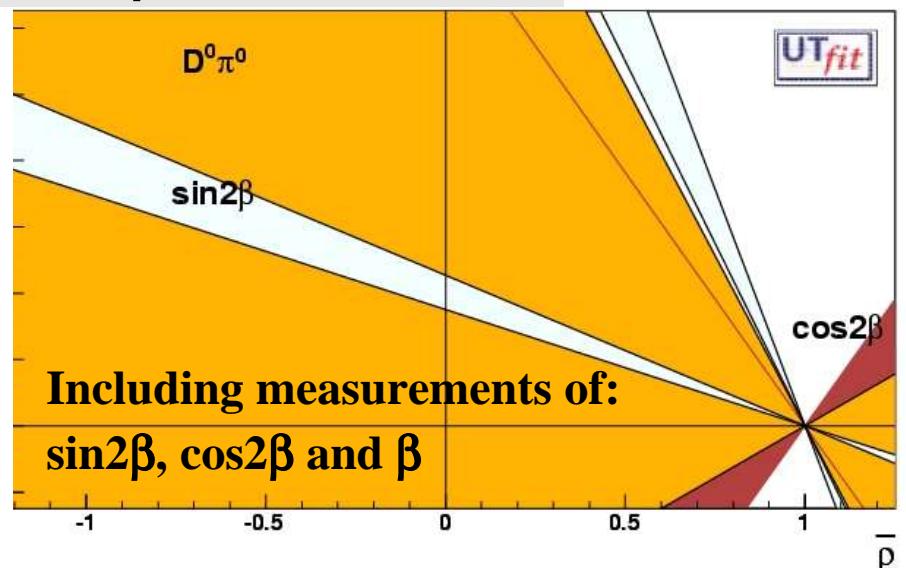
Skeptical combination  
 $\cos 2\beta = 1.9 \pm 1.3$   
 $> 0 @ 87\% \text{ Prob.}$



# $\beta$ from $B^0 \rightarrow D^0\pi^0$



Dalitz plot analysis:  $\beta \rightarrow \beta + \pi$   
Belle result:  $\beta = (16 \pm 24)^\circ$

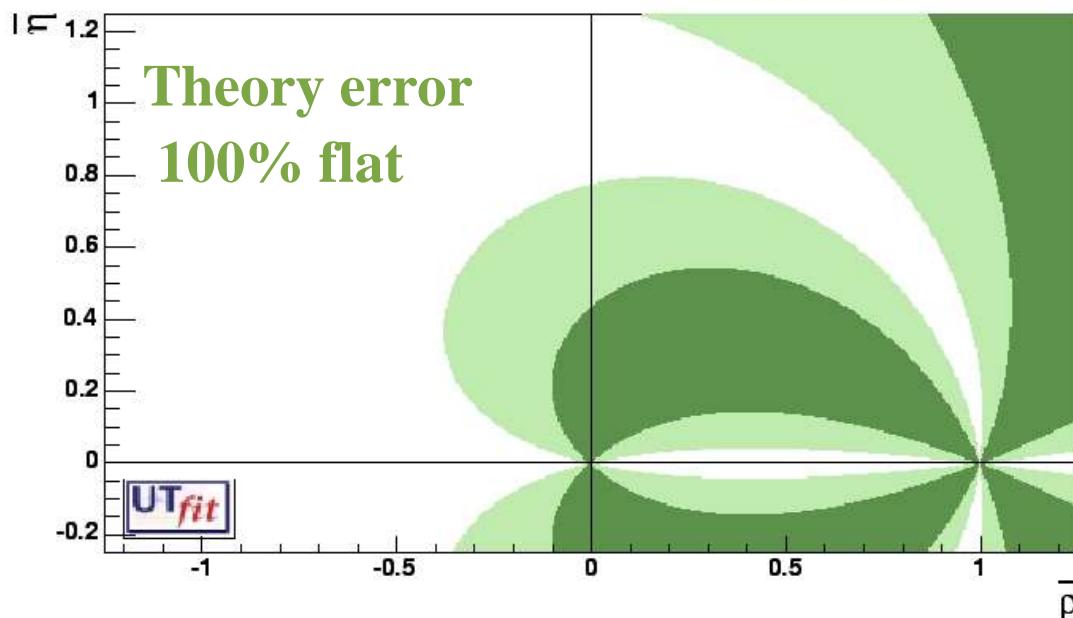
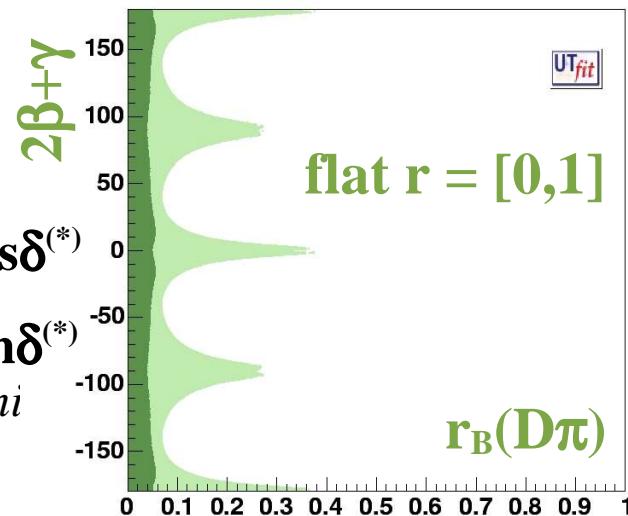


# $2\beta + \gamma$ from $B \rightarrow D^{(*)}\pi(\rho)$

$$a^{(*)} = 2r^{(*)} \sin(2\beta + \gamma) \cos\delta^{(*)}$$

$$c^{(*)} = 2r^{(*)} \cos(2\beta + \gamma) \sin\delta^{(*)}$$

*(leptoni)*



HEP2005, Lisboa, July 21, 2005

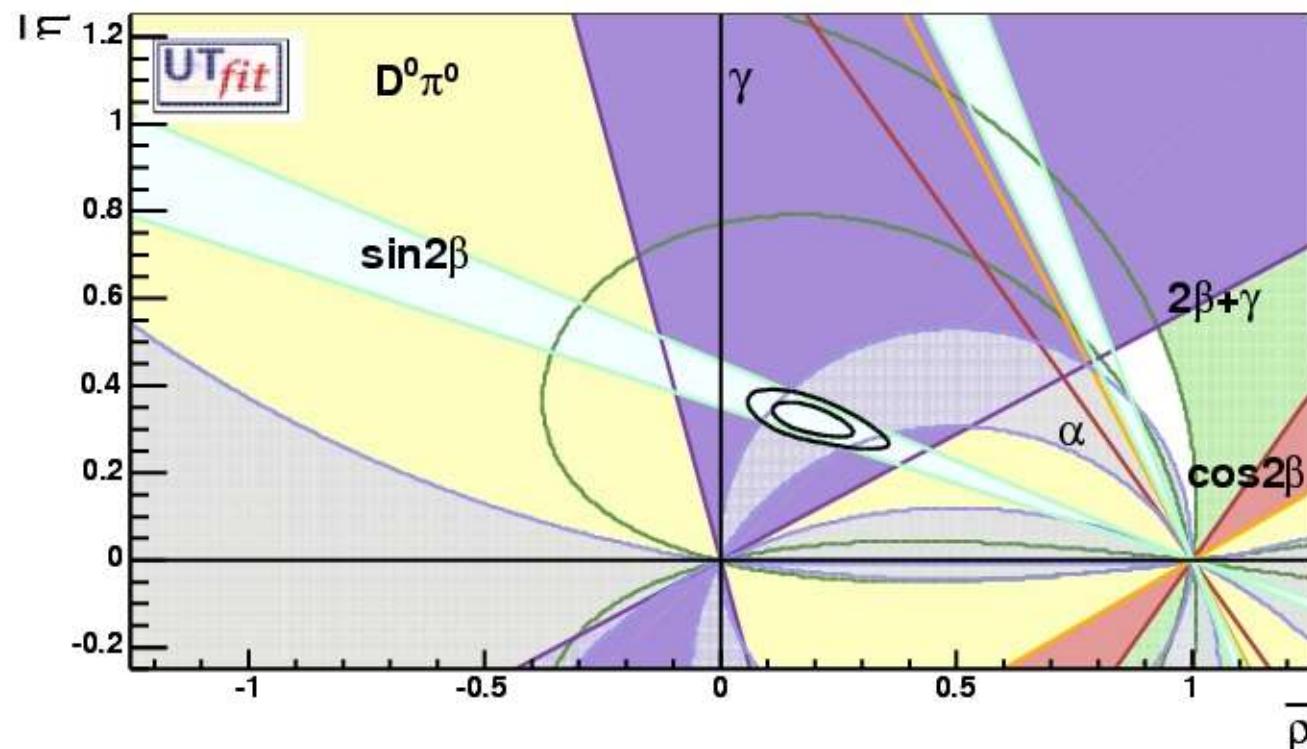
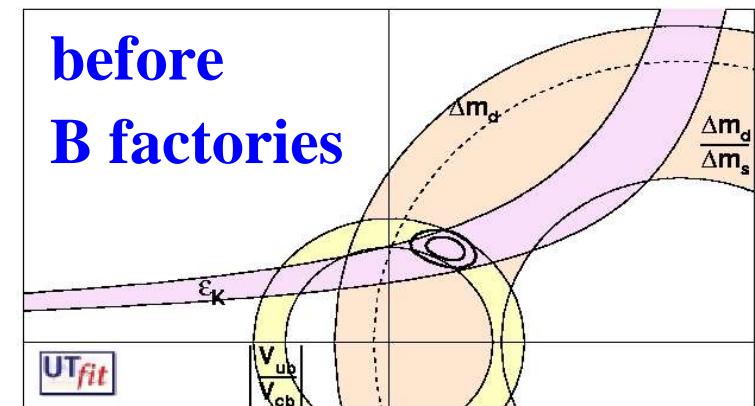
- Interference  $b \rightarrow u$  vs  $b \rightarrow c$  like in  $D\bar{D}$  decays
- Open system: 2 observables for  $2\beta + \gamma$ ,  $r$  and  $\delta$
- Only assuming  $r$  we can extract  $2\beta + \gamma$

- Extraction of  $r$  from  $B \rightarrow D_s\pi$
- Theory error  $\sim 100\%$  flat to take into account SU(3) breaking and annihilations in  $B$  to  $D\pi$

See D. Pirjol, talk at Beauty 2005

# Angles only:

$$\sin 2\beta + \cos 2\beta + \beta + \gamma + \alpha + 2\beta + \gamma$$



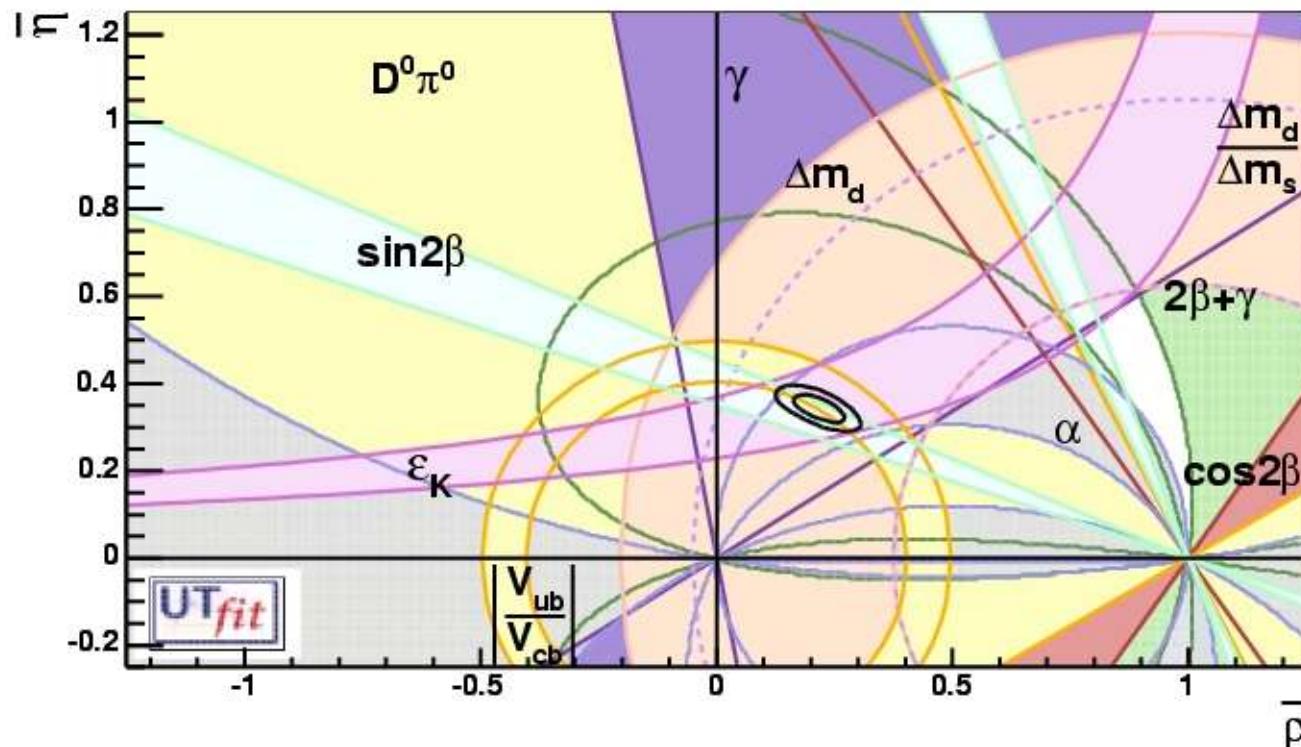
$\bar{\rho} = 0.193 \pm 0.057$   
 $[0.083, 0.321] @ 95\% \text{ Prob.}$

$\bar{\eta} = 0.321 \pm 0.027$   
 $[0.266, 0.376] @ 95\% \text{ Prob.}$

Precision comparable to the analysis in the pre-B-factory era

# Including all the constraints

standard analysis +  $\cos 2\beta$  +  $\beta$  +  $\gamma$  +  $\alpha$  +  $2\beta + \gamma$

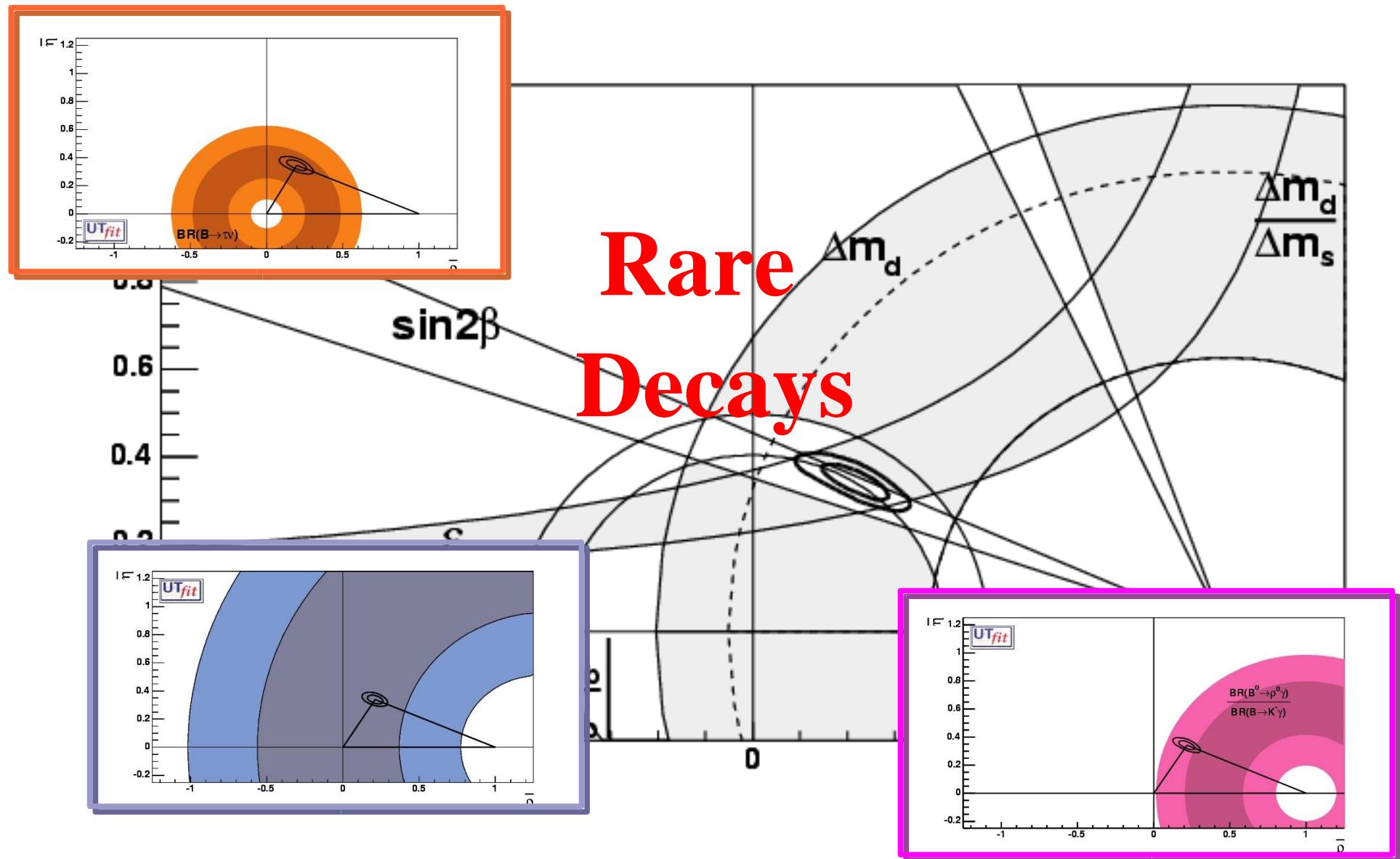


$$\bar{\rho} = 0.216 \pm 0.036$$

$[0.143, 0.288]$  @ 95% Prob.

$$\bar{\eta} = 0.342 \pm 0.022$$

$[0.300, 0.385]$  @ 95% Prob.



$$K^\pm \rightarrow \pi^\pm \nu \bar{\nu}$$

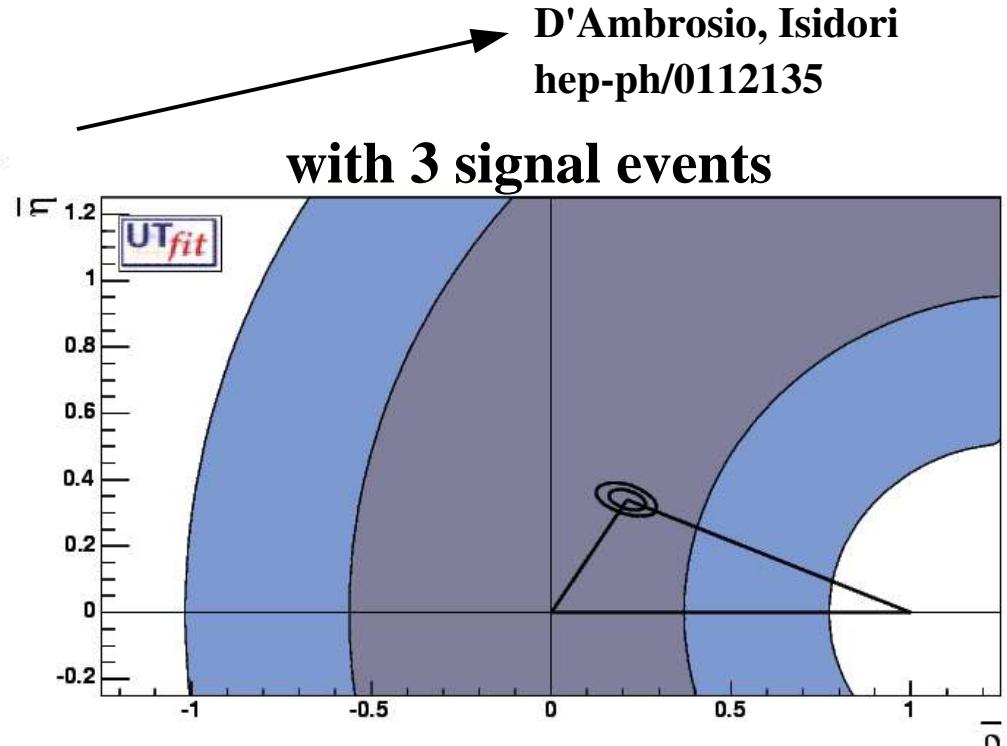
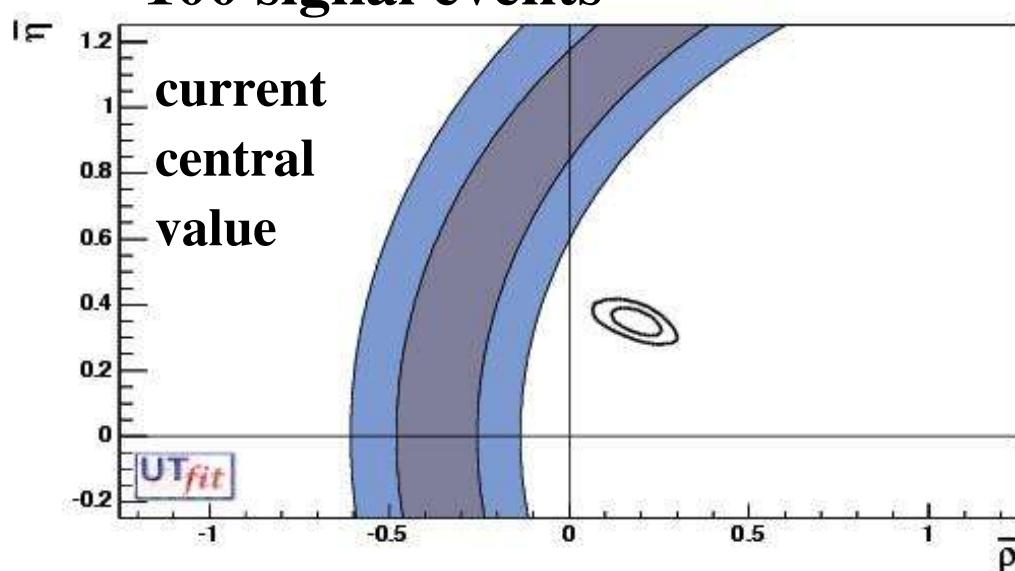
$$\underbrace{(\sigma\bar{\eta})^2 + (\bar{\rho} - \bar{\rho}_0)^2}_{\text{ellipse centered in } (\bar{\rho}^0, 0)} = \frac{\sigma BR(K^+ \rightarrow \pi^+ \nu \bar{\nu})}{\bar{\kappa}_+ |V_{cb}|^4 X^2(x_t)}$$

ellipse centered in  $(\bar{\rho}^0, 0)$

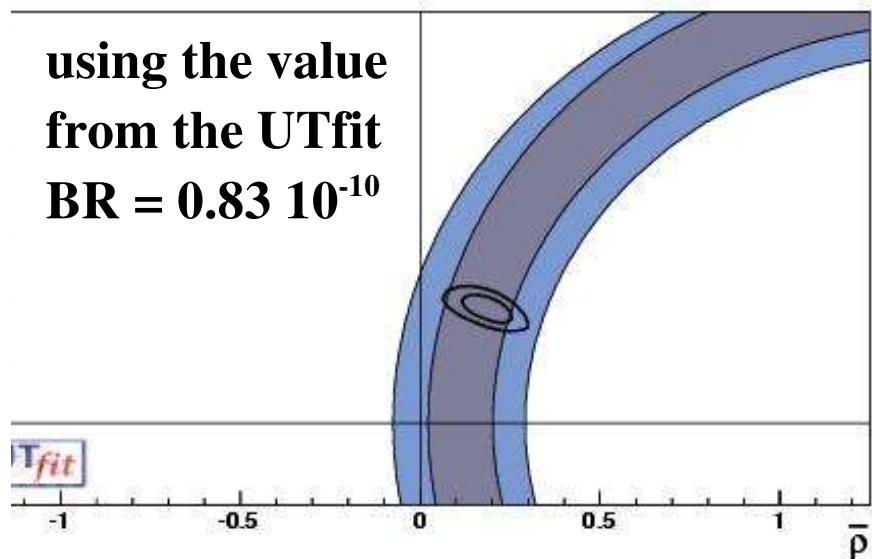
latest result from E949:

$$BR(K^\pm \rightarrow \pi^\pm \nu \bar{\nu}) = 1.47^{+1.30}_{-0.89} 10^{-10}$$

with the hypothesis of  
~100 signal events



using the value  
from the UTfit  
 $BR = 0.83 10^{-10}$



$$\text{BR}(B \rightarrow \rho\gamma) / \text{BR}(B \rightarrow K^*\gamma)$$

$$R = c_\rho^2 \frac{r_m}{\xi^2} \frac{|a_7^c(\rho\gamma)|^2}{|a_7^c(K^*\gamma)|^2} \frac{|V_{td}|^2}{|V_{ts}|^2} (1 + \Delta R)$$

In case of penguin dominance,  $R = \text{BR}(B \rightarrow \rho/\omega\gamma)/\text{BR}(B \rightarrow K^*\gamma)$   
can be used to extract  $|V_{td}/V_{ts}|$ , adding information wrt  $\Delta m_d/\Delta m_s$ .

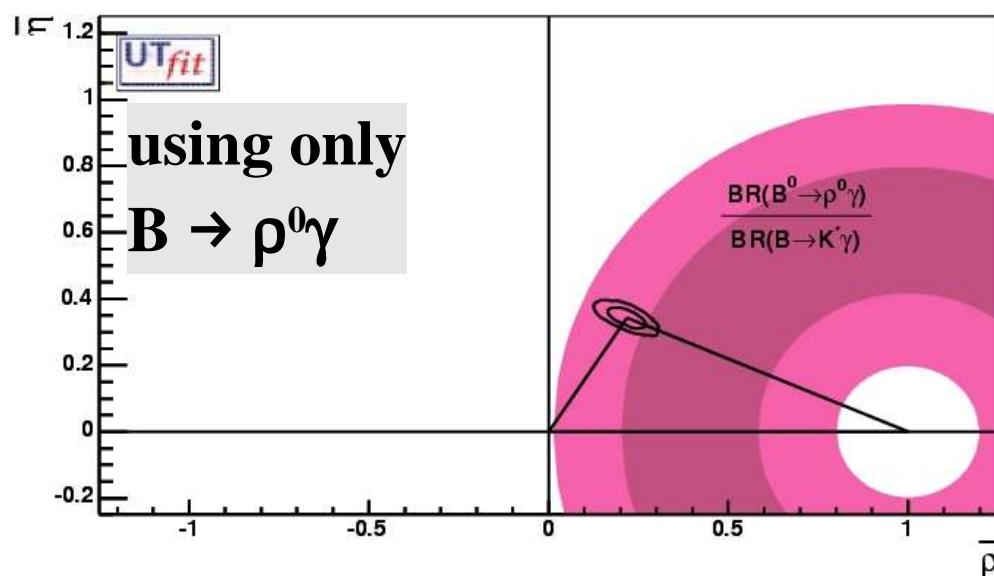
*caveat:* \* SU(3) breaking effect

$$\Delta R \sim O(\Lambda_{\text{QCD}}/m_b)$$

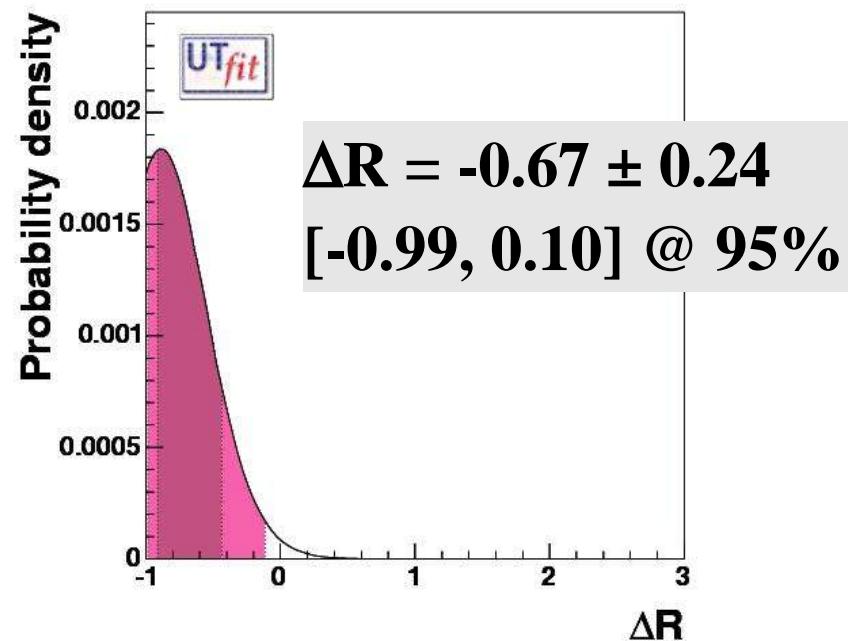
\* annihilation in  $B$  to  $\rho/\omega\gamma$  not in  $B$  to  $K^*\gamma$   
associated to a different CKM factor ( $\sim V_{ub}^* V_{ud}$ )

## QCD factorisation

$$|V_{td}/V_{ts}| = 0.10 \pm 0.45  
[0.02, 0.18] @ 95\% \text{ Prob.}$$

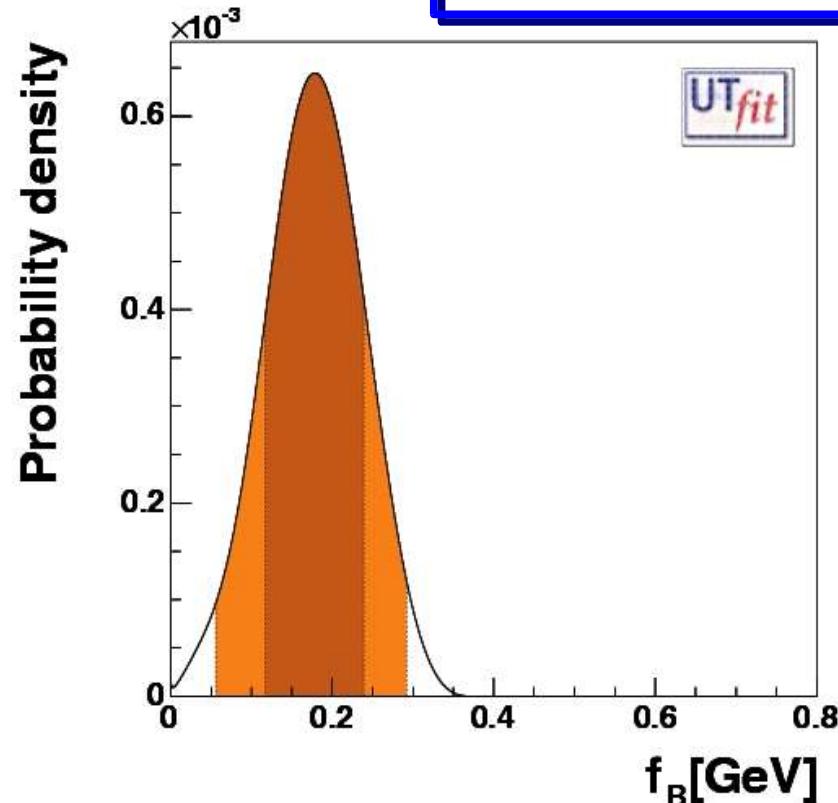


Using the  $|V_{td}/V_{ts}|$  value from the SM, we can extract  $\Delta R$ .



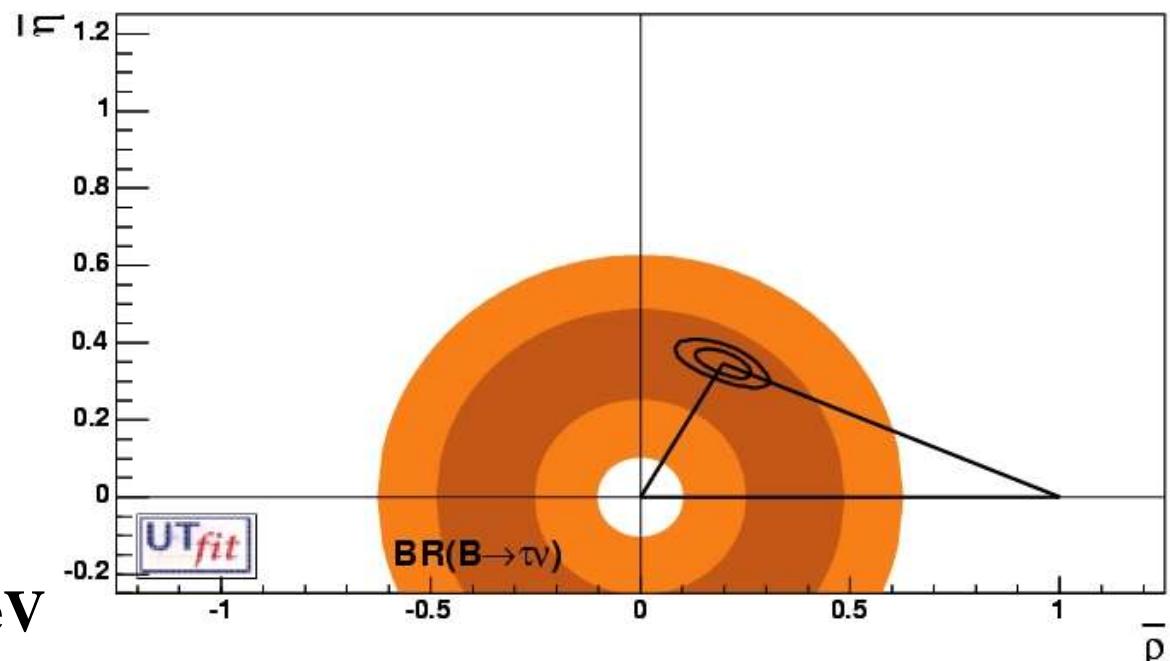
**$B \rightarrow \tau\nu$** 

$$\mathcal{B}(B \rightarrow \ell\nu) = \frac{G_F^2 m_B m_\ell^2}{8\pi} \left(1 - \frac{m_\ell^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2 \tau_B$$

 **$< 1.8 \cdot 10^{-4}$  @ 90% CL** $f_{Bd} = 0.178 \pm 0.062$  GeV $f_{Bd} = 0.192 \pm 0.026 \pm 0.009$  GeV

from lattice QCD

Assuming  $f_B$ :  
**Constraint on  $R_b = \bar{\rho}^2 + \bar{\eta}^2$**   
 $R_b = 0.37 \pm 0.13$



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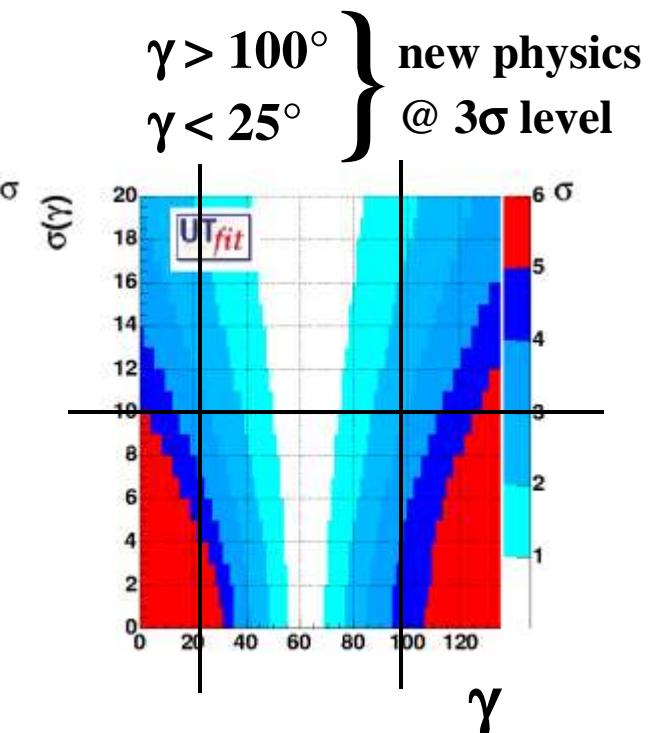
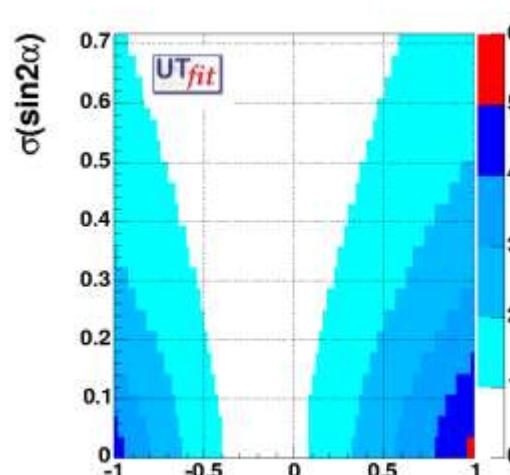
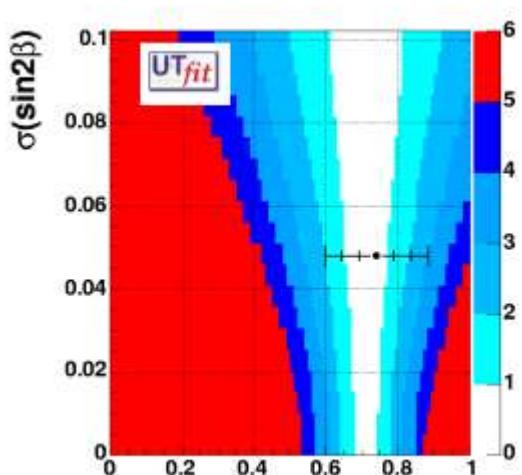
[www.utfit.org](http://www.utfit.org)



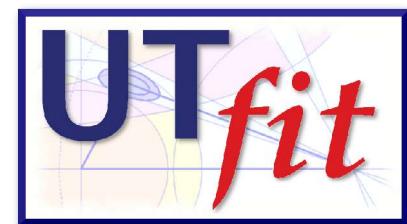
# Back up slides

# Compatibility plots:

**red:  $5\sigma$  exclusion zone**

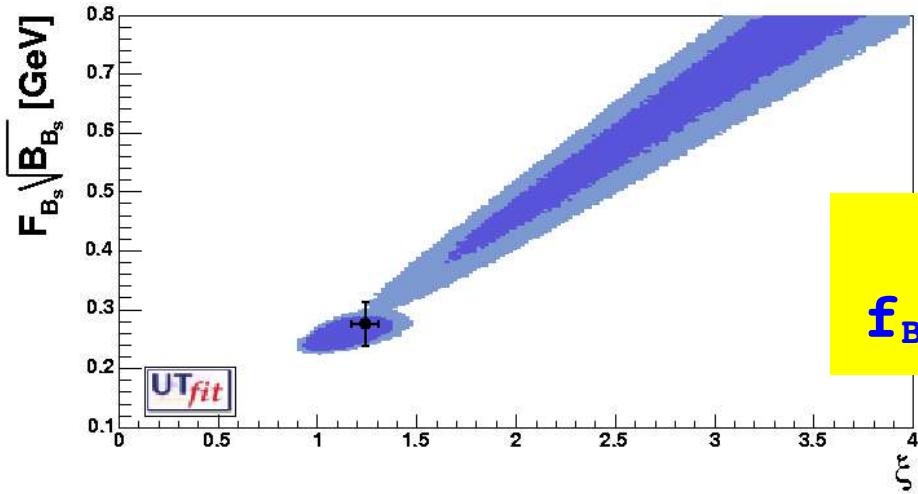
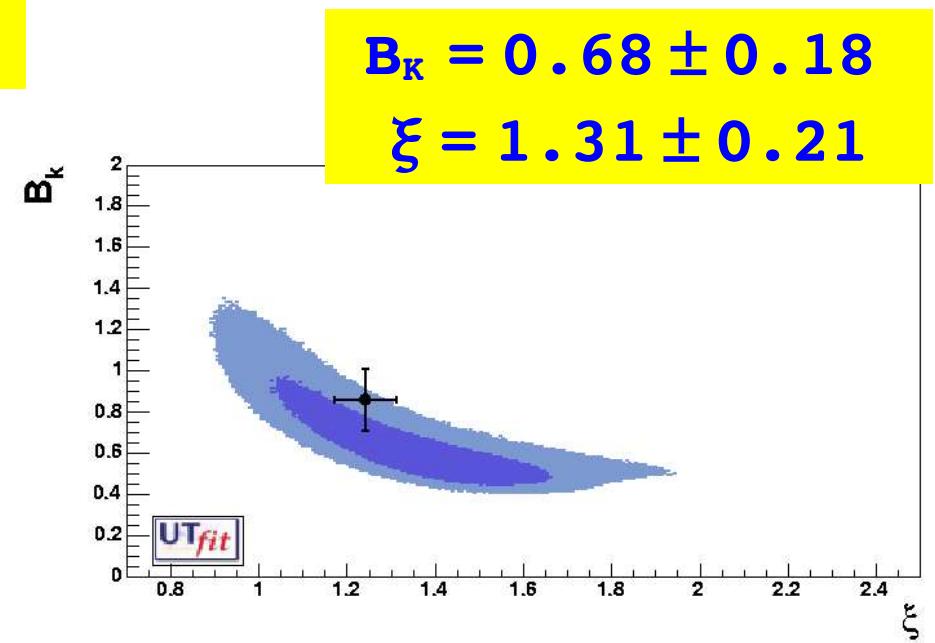
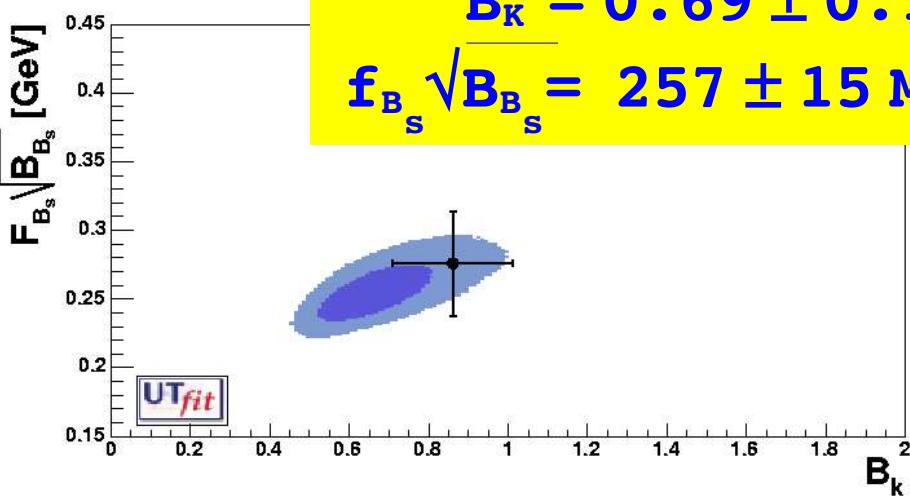


**comparison between the indirect determination  
and a (hypothetical) direct  
experimental determination**





## and LQCD predictions (II)



dark: 65%  
light: 95%

## $\alpha$ dall'analisi di isospin (II): $\pi\pi$

UTfit method: integrating over T, P,  $T_\delta$ ,  $\delta_P$ ,  $\delta_{T_c}$

**HFAG**  
Moriond 2005

$$\begin{aligned} S_{\pi\pi} &= -0.50 \pm 0.12 \\ C_{\pi\pi} &= -0.37 \pm 0.10 \end{aligned}$$

